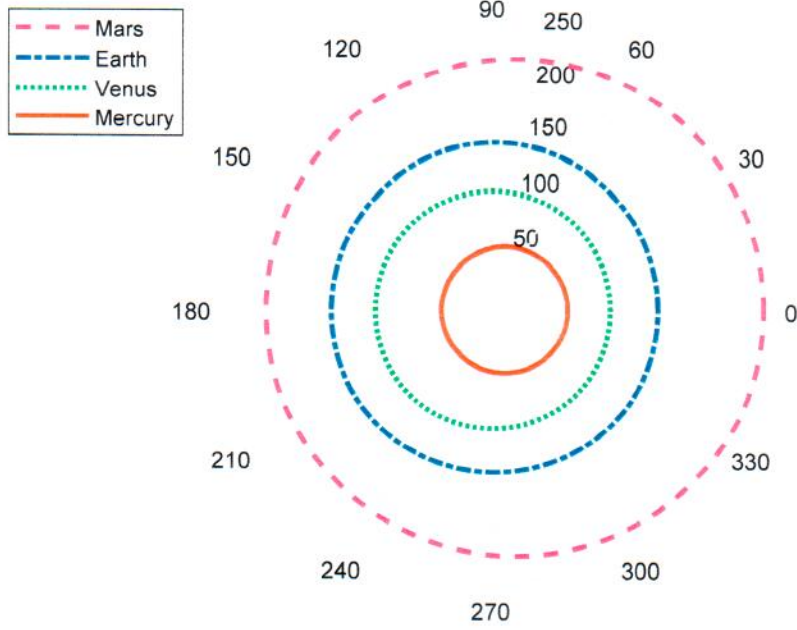
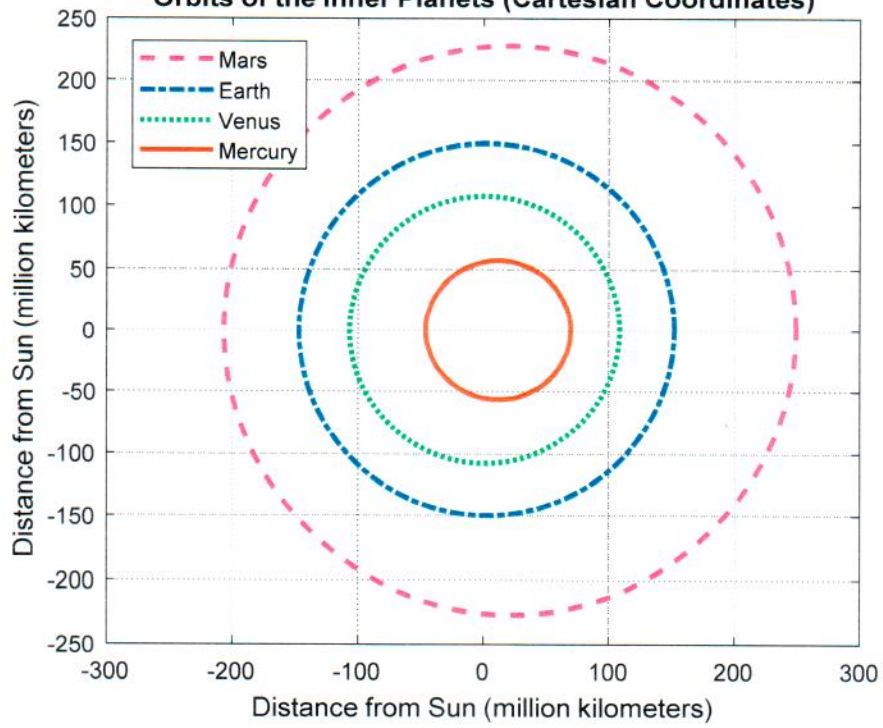


Orbits of the Inner Planets (Polar Coordinates with r in 10^6 km)



Orbits of the Inner Planets (Cartesian Coordinates)



```
ORBITS_1.M   Plots Orbits of the Inner Planets
```

This HW illustrates several aspects of programming within the Matlab environment. The goal here is simply to evaluate and plot the orbits of the four inner planets of our solar system. This will use a 2-D array for storage of information, and address plotting the orbits on Cartesian and polar coordinate axes. The proper use of 'dot arithmetic' is critical here...

Reference: This problem came from Prob. 5.15 in the book, Matlab - An Introduction With Applications, by A. Gilat (2004). Note that the units of P are in millions of kilometers.

File prepared by J. R. White, UMass-Lowell (last update: Sept. 2017)

```
clear all, close all, nfig = 0;
```

```
define the orbital constants for four planets (mercury, venus, earth, & mars)
P = [269.2 15913 8964 2421];           % P values (10^6 km)
e = [0.206 0.00677 0.0167 0.0934];    % eccentricity (unitless)
Np = length(P);                       % number of planets
```

```
define theta vector and initialize 2-D array for function values
Nth = 181; thd = linspace(0,360,Nth)'; thr = thd*pi/180; r = zeros(Nth,Np);
```

```
loop over number of planets and compute r vs thr for each planet
for j = 1:Np
    r(:,j) = e(j)*P(j)./(1 - e(j)*cos(thr));
end
```

```
as a quick sanity check, calc the average radius of the earth from the sun and
compare to the 'known value' of about 93 million miles (result = 93.04 -- OK)
cf = 1.60934;                          % conversion factor (km/mile)
EarthR = mean(r(:,3))/cf;               % ave earth-sun distance in 10^6 miles
disp('Average radius from sun to earth in millions of miles: '); disp(EarthR)
```

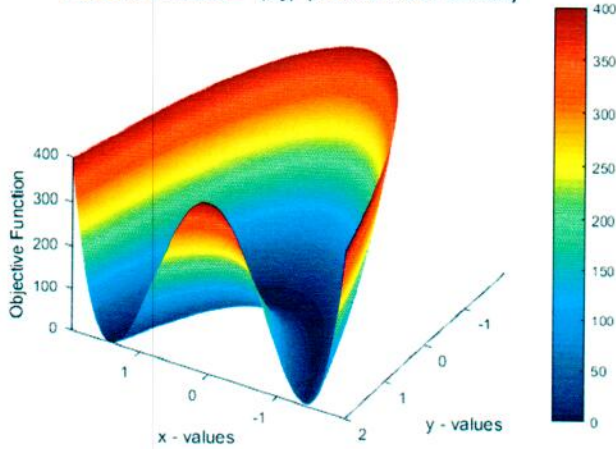
```
create polar plot of the orbits
ss = ['r- '; 'g: '; 'b-.'; 'm--'];
nfig = nfig+1; figure(nfig)
for j = Np:-1:1 % reverse order because Matlab had scaling problems
    h = polar(thr,r(:,j),ss(j,:));hold on;
    set(h,'LineWidth',2) % increase the line width for better visualization
end
legend('Mars','Earth','Venus','Mercury','Location','NorthWest')
title('Orbits of the Inner Planets (Polar Coordinates with r in 10^6 km)')
```

```
chk = 0; % chk = 1, do forward order just to check current Matlab version
if chk == 1
    nfig = nfig+1; figure(nfig)
    for j = 1:Np
        h = polar(thr,r(:,j),ss(j,:));hold on;
        set(h,'LineWidth',2) % increase the line width for better visualization
    end
end
```

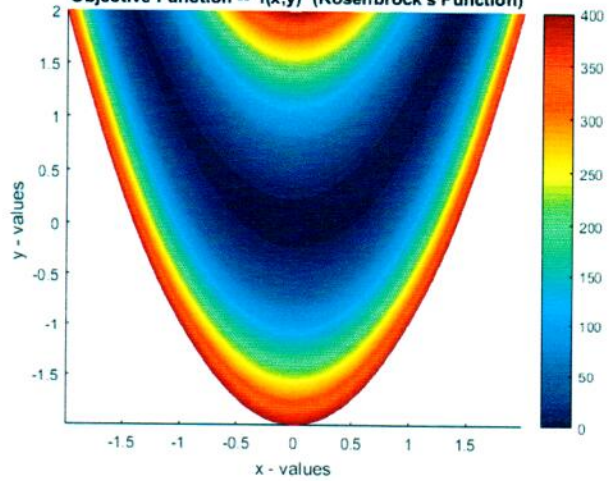
```
% create x,y plot of the orbits (keep same order as above for consistency)
nfig = nfig+1; figure(nfig)
for j = Np:-1:1
    x = r(:,j).*cos(thr); y = r(:,j).*sin(thr);
    plot(x,y,ss(j,:), 'LineWidth',2),grid on,hold on,axis equal
end
xlim([-300 300]); ylim([-250 250]);
xlabel('Distance from Sun (million kilometers)')
ylabel('Distance from Sun (million kilometers)')
legend('Mars','Earth','Venus','Mercury','Location','NorthWest')
title('Orbits of the Inner Planets (Cartesian Coordinates)')
%
end of program
```

Objective Function #3 Results

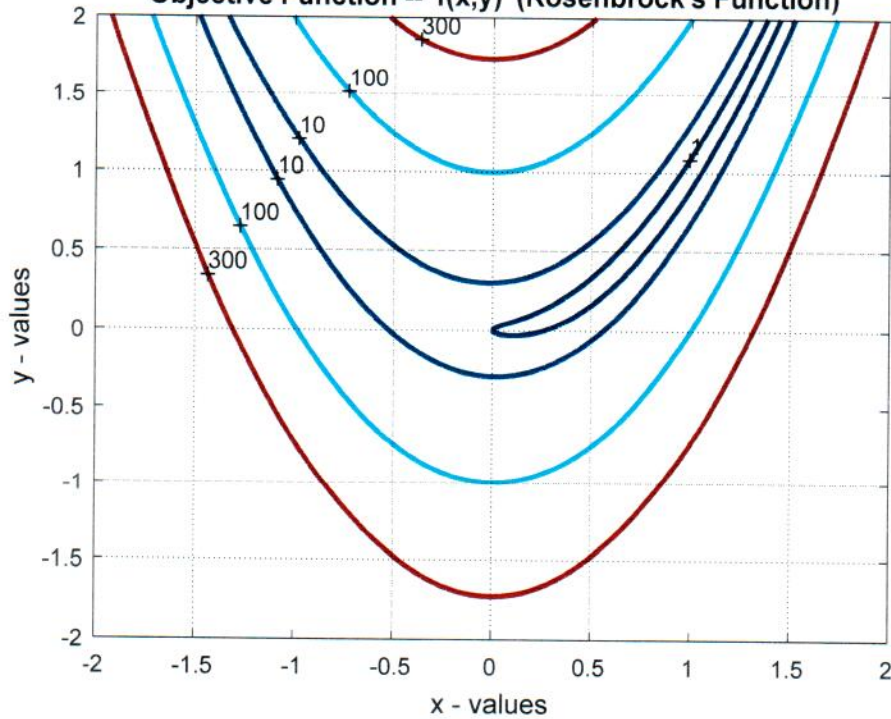
Objective Function -- $f(x,y)$ (Rosenbrock's Function)



Objective Function -- $f(x,y)$ (Rosenbrock's Function)



Objective Function -- $f(x,y)$ (Rosenbrock's Function)



```
>> obj_func_3
```

```
Minimum value of the objective function: 0.0000
```

```
x - location of minimum of f: 1.0000
```

```
y - location of minimum of f: 1.0000
```

```

%
% OBJ_FUNC_3.M      Function evaluation and 3-D plotting in Matlab
%
% Plot f(x,y) = 100*(y - x^2)^2 + (1 - x)^2  to find local minimum
%
% This file computes and plots the objective function f(x,y).  The goal here is
% to visualize the functional behavior and to find any minima that may occur.
% Matlab has a variety of capabilities here, and several alternatives are used to
% view this two-dimensional function using the surf and contour commands.
%
% This function is the well-known Rosenbrock function that is used in studying
% optimization methods.  Although this function has an obvious minimum at x = y = 1,
% we actually use Matlab's fminsearch to find this value (just to illustrate its
% use)...
%
% File prepared by J. R. White, UMass-Lowell  (last update: Sept. 2017)
%
%
% clear all,  close all,  nfig = 0;
%
% identify basic problem data
% x = -2:0.004:2;  Nx = length(x);          % range for x
% y = -2:0.005:2;  Ny = length(y);          % range for y
% [xx,yy] = meshgrid(x,y);                  % matrix of independent variables
%
% compute objective function (be careful with "dot" arithmetic)
% f = 100*(yy - xx.^2).^2 + (1 - xx).^2;
% f(f > 400) = nan;                          % eliminate region where f > 400
%
% now plot the function in a number of ways
% nfig = nfig+1;  figure(nfig)
% surf(xx,yy,f), shading interp; colorbar, colormap jet
% title('Objective Function -- f(x,y) (Rosenbrock''s Function)')
% xlabel('x - values'),ylabel('y - values'),zlabel('Objective Function')
% axis tight
%
% nfig = nfig+1;  figure(nfig)
% surf(xx,yy,f), view(-150,45), shading interp; colorbar, colormap jet
% title('Objective Function -- f(x,y) (Rosenbrock''s Function)')
% xlabel('x - values'),ylabel('y - values'),zlabel('Objective Function')
% axis tight
%
% nfig = nfig+1;  figure(nfig),
% surf(xx,yy,f), view(2), shading interp; colorbar, colormap jet
% title('Objective Function -- f(x,y) (Rosenbrock''s Function)')
% xlabel('x - values'),ylabel('y - values'),zlabel('Objective Function')
% axis tight
%
% nfig = nfig+1;  figure(nfig)
% vc = [1 10 100 300];
% [con,han] = contour(xx,yy,f,vc); grid, colormap jet
% clabel(con), set(han,'LineWidth',2)
% title('Objective Function -- f(x,y) (Rosenbrock''s Function)')
% xlabel('x - values'),ylabel('y - values')
%
% nfig = nfig+1;  figure(nfig)

```

```

vc = [0.01 0.1 1 ];
[con,han] = contour(xx,yy,f,vc); grid, colormap jet
clabel(con), set(han,'LineWidth',2)
r = [0.5 1.5 0.5 1.5]; axis(r)
title('Objective Function -- f(x,y) (Rosenbrock''s Function)')
xlabel('x - values'),ylabel('y - values')

```

the contour plot clearly shows a distinct minimum in the region around $x = y = 1$.
just for fun, let's use `fminsearch` to formally find this minimum

```

fz = @(z) 100*(z(2) - z(1)^2)^2 + (1 - z(1))^2;
[locm,fm] = fminsearch(fz,[0.5 0.5]); % use x = y = 0.5 as a starting guess
fprintf('Minimum value of the objective function: %8.4f \n',fm);
fprintf('x - location of minimum of f:           %8.4f \n',locm(1));
fprintf('y - location of minimum of f:           %8.4f \n\n',locm(2));

```

% end of problem