CHEN.3170 Applied Engineering Problem Solving

A Short Quiz on Implementation of Discrete Equations within a Matlab Function

The Gauss Elimination method for solving a system of linear algebraic equations is a two-step process. The first step performs row operations to put the original system of equations into "row echelon" or "upper triangular" form. Once the system is in this form, a relatively simple process known as "back substitution" will give the desired solution vector.

A discrete representation of the back-substitution process for solving $\underline{\underline{U}}\underline{x} = \underline{z}$ can be written for the general case of N equations as follows:

$$x_{N} = \frac{z_{N}}{u_{NN}}$$
 and $x_{i} = \frac{1}{u_{ii}} \left(z_{i} - \sum_{j=i+1}^{N} u_{ij} x_{j} \right)$ for $i = N - 1, N - 2, \dots, 1$

Your job is to write a complete Matlab function file that implements this discrete procedure. The function receives the upper triangular matrix, \underline{U} , and right hand side vector, \underline{z} , from the main program and returns the solution vector, \underline{x} , to the calling routine. For consistency, assume that the first line of the function file is given by

function x = backsub(U, z)

Be careful to use proper Matlab syntax in your program!