## CHEN. 3030 Fluid Mechanics

## Homework Assignment \#10 Spring 2017

Pipe Flow Applications

1. Consider a solar collector that is 1 m wide and 5 m long and has a constant spacing of 3 cm between the glass cover and the collector plate. Air flows within the rectangular channel at an average temperature of 45 C at a rate of $0.15 \mathrm{~m}^{3} / \mathrm{s}$ as shown in the sketch.

Disregarding the entrance and roughness effects, estimate the pressure drop in the collector.

2. A positive displacement pump delivers an essentially constant discharge flow rate independent of the discharge pressure. In a particular flow system, with the suction pressure of the pump fixed at 10 psig , the desired water flow rate is $250 \mathrm{gal} / \mathrm{min}$. The water temperature is 60 F and the horizontal Schedule 40 discharge line is 200 ft long. The pipe exit is open to the atmosphere. Assume that the suction line has a relatively short $31 / 2^{\prime \prime}$ Schedule 40 commercial steel pipe ( $\mathrm{D}_{3.5}=0.2957 \mathrm{ft}$ ).
a. Compute the power added by the pump (in hp) if the discharge line is a $2^{\prime \prime}$ Schedule 40 steel pipe ( $\mathrm{D}_{2}=0.1723 \mathrm{ft}$ ).
b. Now, redo the calculation from Part a using your favorite computer analysis tool (Excel, Matlab, Mathcad, etc.). Validate the computer calculations using your hand calculations for the $2^{\prime \prime}$ Schedule 40 discharge line as a benchmark case.
Once you get this working, redo the calculations using both $21 / 2^{\prime \prime}$ and $3^{\prime \prime}$ Schedule 40 commercial steel pipes ( $\mathrm{D}_{2.5}=0.2058 \mathrm{ft}^{2}$ and $\mathrm{D}_{3}=0.2557 \mathrm{ft}^{2}$, respectively). With these data, discuss how the power delivered by the pump changes versus discharge line size. How does this tradeoff affect the cost of a given piping system?
3. A vented tanker is to be filled with fuel oil ( $\rho=920 \mathrm{~kg} / \mathrm{m}^{3}$ and $\mu=0.045 \mathrm{~kg} / \mathrm{m}-\mathrm{s}$ ) from a vented underground reservoir using a 20 m long, 5 cm diameter, smooth plastic hose. The connection to the reservoir has a slightly rounded entrance ( $\mathrm{K}=0.12$ ) and the hose to the tanker has two smooth $90^{\circ}$ bends ( $\mathrm{K}=0.3$ for each bend). The elevation difference between the oil level in the reservoir and the top of the tanker where the hose is connected is 5 m (note that the hose exit is a free jet). A pump in the system between the reservoir and the tanker provides a constant flow rate of $0.01 \mathrm{~m}^{3} / \mathrm{s}$.

Assuming an overall pump efficiency of 82 percent, determine the required power input to the pump to operate this system.
4. Estimate the discharge of oil in gallon/min (gpm) in the configuration shown in the sketch. Assume a sudden contraction at the tank-pipe interface and that the gate valve has a resistance coefficient $\mathrm{K}=5.6$. Note that this is a Type II problem!

5. Manufacturer data for a small aquarium pump are given below:

| Flow Rate $\left(\mathbf{m}^{3} / \mathbf{s}\right)$ | 0 | $1 \mathrm{e}-6$ | $2 \mathrm{e}-6$ | $3 \mathrm{e}-6$ | $4 \mathrm{e}-6$ | $5 \mathrm{e}-6$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Head (m) | 1.10 | 1.00 | 0.80 | 0.60 | 0.35 | 0.0 |

Using this pump, what is the flow rate achieved in the system shown in the diagram? The tubing between the two reservoirs is a smooth plastic material with an inside diameter of 0.5 cm and a total length of 29.8 m . The water is at room temperature. Minor
 losses can be ignored.

