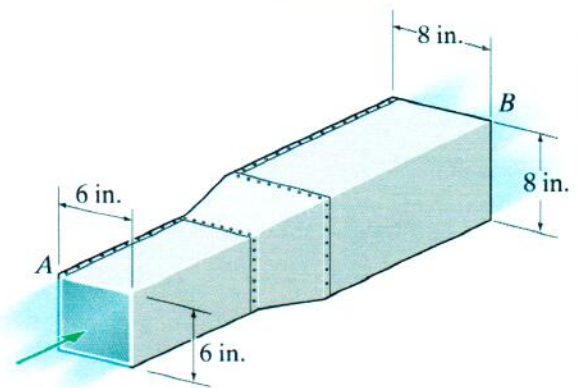


Air at 100 °F flows through the square horizontal duct section at Point A at 200 ft/s under a pressure of 1.50 psi.

Determine the pressure in the square duct section at Point B.



Write Bernoulli Eqn from A to B

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B$$

- $z_A = z_B$
- $P_A = 1.50 \text{ psi}$
- $V_A = 200 \text{ ft/s}$
- assume
- ① incompressible
- ② no friction

$$P_B = P_A + \frac{\gamma}{2g} (V_A^2 - V_B^2)$$

$$P_B = P_A + \frac{\rho}{2} (V_A^2 - V_B^2)$$

But from the continuity eqn for incompressible flow

$$Q_A = Q_B$$

$$V_A A_A = V_B A_B \Rightarrow V_B^2 = V_A^2 \left(\frac{A_A}{A_B} \right)^2$$

$$\therefore P_B = P_A + \frac{\rho}{2} \left(1 - \frac{A_A^2}{A_B^2} \right) V_A^2$$

$$A_A^2 = (36 \text{ in}^2)^2 = 1296 \text{ in}^4$$

$$A_B^2 = (64 \text{ in}^2)^2 = 4096 \text{ in}^4$$

Now let's insert the values

$$\rho_{\text{air}} = 0.00220 \frac{\text{slugs}}{\text{ft}^3}$$

$$P_B = 1.50 \frac{\text{lb}}{\text{in}^2} + \left(\frac{0.00220 \text{ slugs}}{2 \text{ ft}^3} \right) \left(1 - \frac{1296}{4096} \right) \left(200 \frac{\text{ft}}{\text{s}} \right)^2$$

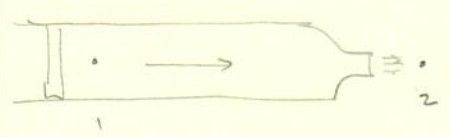
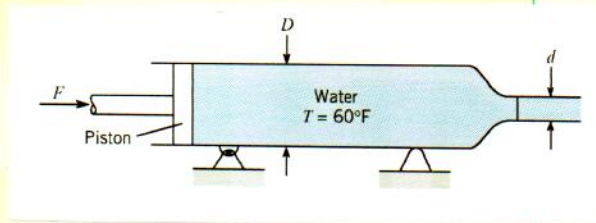
$$= 1.50 \frac{\text{lb}}{\text{in}^2} + 30.08 \frac{\text{lb}}{\text{ft}^2} \times \frac{1 \text{ ft}^2}{144 \text{ in}^2}$$

$$= 1.50 + 0.209$$

or $P_B \approx 1.71 \text{ psi}$ ans

Hibbeler
 Prob A

5.52 Water is forced out of the cylinder shown in the diagram. If the piston is driven at a speed of 4 ft/s, what will be the average exit velocity of the water if $d = 2$ in and $D = 4$ in? Also estimate the force that will be required to drive the piston.



Bernoulli eqn from ① to ②

$$\frac{P_1}{\rho} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho} + \frac{V_2^2}{2g} + z_2$$

← free stream
↖ horizontal ↗

$$\therefore \frac{P_1}{\rho} = \frac{V_2^2 - V_1^2}{2g}$$

Continuity Eqn

$$Q_1 = Q_2 \quad \therefore V_2 = \frac{V_1 A_1}{A_2} = \frac{(4 \text{ ft/s}) \frac{\pi}{4} (4 \text{ in})^2}{\frac{\pi}{4} (2 \text{ in})^2}$$

$$V_2 = 16 \text{ ft/s} \quad \text{ans}$$

now put this into the Bernoulli Eqn ← water 60°F

$$P_1 = \frac{\rho (V_2^2 - V_1^2)}{2} = \frac{1.94 \text{ slug}}{\text{ft}^3} \frac{(16^2 - 4^2) \text{ ft}^2/\text{s}^2}{2}$$

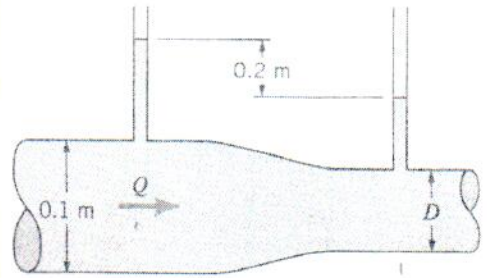
$$1 \text{ lbf} = 1 \text{ slug} \frac{\text{ft}}{\text{s}^2}$$

$$= 232.8 \frac{\text{slug}}{\text{ft}^3} \frac{\text{ft}^2}{\text{s}^2} \left(\frac{\text{ft}}{\text{ft}} \right) = \boxed{232.8 \frac{\text{lbf}}{\text{ft}^2}} \times \frac{1 \text{ ft}^2}{144 \text{ in}^2}$$

$$P_1 = 1.62 \text{ psi}$$

$$\therefore F_1 = P_1 A_1 = \left(1.62 \frac{\text{lbf}}{\text{in}^2} \right) \left(\frac{\pi}{4} (4 \text{ in})^2 \right) = \boxed{20.3 \text{ lbf}} \quad \text{ans}$$

3.31 Water flows through the pipe contraction as shown. For the given 0.2 m difference in the manometer level, determine the flow rate, Q , in the pipe if $D = 0.05$ m. Neglect viscous effects.



First identify the upstream and downstream locations of the manometer tubes as pt 1 and pt 2.

Now applying the Bernoulli eqn., we have

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 \quad \left\{ \text{where } z_1 = z_2 = 0 \right.$$

thus,
$$\frac{P_1 - P_2}{\gamma} = \frac{V_2^2 - V_1^2}{2g}$$

From the continuity eqn

$$Q_1 = Q_2 \quad \sim \quad V_2 = \frac{A_1}{A_2} V_1 = \left(\frac{D_1}{D_2} \right)^2 V_1$$

Putting this result into the reduced Bernoulli eqn gives

$$\frac{\left[\left(\frac{D_1}{D_2} \right)^4 - 1 \right] V_1^2}{2g} = \frac{P_1 - P_2}{\gamma}$$

$$\text{or } V_1 = \left[\frac{2g(P_1 - P_2)}{\gamma} \right]^{1/2} \left[\left(\frac{D_1}{D_2} \right)^4 - 1 \right]^{-1/2}$$

from the manometer $P_1 - P_2 = (0.2 \text{ m}) \gamma$

from the dimension given

$$\frac{D_1}{D_2} = \frac{0.1}{0.05} = 2$$

$$\left. \begin{array}{l} P_1 = \gamma h_1 \\ P_2 = \gamma h_2 \\ P_1 - P_2 = \gamma(h_1 - h_2) \end{array} \right\} \begin{array}{l} \therefore \left[\left(\frac{D_1}{D_2} \right)^4 - 1 \right]^{-1/2} = \frac{1}{\sqrt{15}} \\ = 0.2582 \end{array}$$

$$\therefore V_1 = \left[2 \left(9.8 \frac{\text{m}}{\text{s}^2} \right) (0.2 \text{ m}) \right]^{1/2} (0.2582)$$

$$V_1 = 0.511 \text{ m/s}$$

and $Q = A_1 V_1 = \frac{\pi}{4} (0.1 \text{ m})^2 (0.511 \text{ m/s}) = 4.01 \times 10^{-3} \frac{\text{m}^3}{\text{s}}$

13,782
42,381
42,382
42,389
42,399
Made in U.S.A.

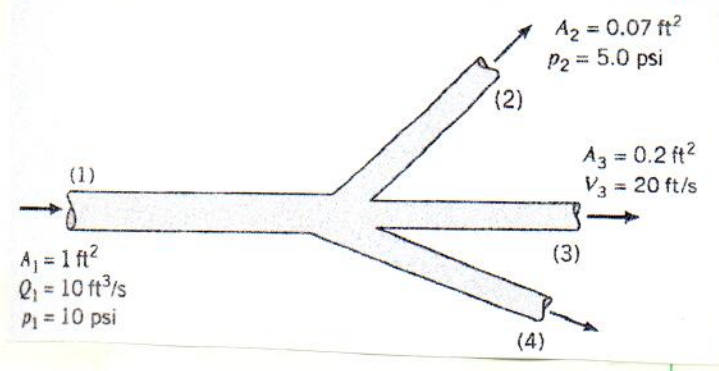


12 795
42 381
42 382
42 389
42 395
100 SHEETS FILER SQUARE
50 SHEETS EYE-EASER SQUARE
200 SHEETS EYE-EASER SQUARE
200 SHEETS EYE-EASER SQUARE
200 SHEETS EYE-EASER SQUARE
200 SHEETS EYE-EASER SQUARE
200 SHEETS EYE-EASER SQUARE



from continuity eqn
 $Q_4 = Q_1 - Q_2 - Q_3 = 10 - 2.03 - 4 = 3.97 \text{ ft}^3/\text{s}$

3.82) Water flows through the horizontal branching pipe shown at a rate of $10 \text{ ft}^3/\text{s}$. If viscous effects are negligible, determine the water speed at section 2, the pressure at section 3, and the flow rate at section 4.



a) Bernoulli Eqn between ① and ②

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2$$

$$\frac{V_2^2}{2g} = \frac{V_1^2}{2g} + \frac{P_1 - P_2}{\gamma}$$

$$V_1 = \frac{Q}{A_1} = \frac{10 \text{ ft}^3/\text{s}}{1 \text{ ft}^2} = 10 \text{ ft/s}$$

$$V_2 = \left[V_1^2 + \left(\frac{P_1 - P_2}{\gamma} \right) (2g) \right]^{1/2}$$

$$V_1 = 10 \text{ ft/s}$$

$$= \left[(10 \text{ ft/s})^2 + \frac{(10 - 5) \frac{\text{lbf}}{\text{in}^2} \cdot \frac{144 \text{ in}^2}{\text{ft}^2}}{\left(\frac{62.4 \text{ lbf}}{\text{ft}^3} \right)} \times 2 \times 32.2 \text{ ft/s}^2 \right]^{1/2}$$

$$= \left[100 + \frac{5(144)(2)(32.2)}{62.4} \text{ ft}^2/\text{s}^2 \right]^{1/2} = \left[100 + 743 \right]^{1/2}$$

$$V_2 = 29 \text{ ft/s} \text{ ans}$$

also $Q_2 = V_2 A_2 = (29 \text{ ft/s})(0.07 \text{ ft}^2) = 2.03 \text{ ft}^3/\text{s}$

b) Bernoulli eqn between ① and ③

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_3}{\gamma} + \frac{V_3^2}{2g} + z_3$$

$$P_3 = P_1 + \gamma \left(\frac{V_1^2 - V_3^2}{2g} \right)$$

$$= (10) \left(\frac{144 \text{ lbf}}{\text{ft}^3} \right) + \frac{62.4 \text{ lbf/ft}^3}{2(32.2) \text{ ft/s}^2} \left[(10 \text{ ft/s})^2 - \left(\frac{20 \text{ ft}}{5} \right)^2 \right]$$

$$= (1440 - 290.7) \text{ lbf/ft}^2$$

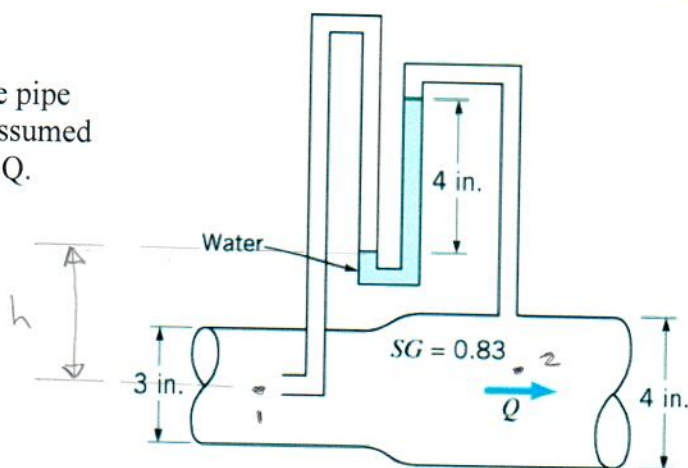
water
 $\gamma = \rho g = \left(\frac{1.94 \text{ slug}}{\text{ft}^3} \right) \left(32.174 \frac{\text{ft}}{\text{s}^2} \right) = 62.4 \text{ lbf/ft}^3$

$$P_3 = 1149.3 \frac{\text{lbf}}{\text{ft}^2} = 7.98 \text{ psi ans}$$

also $Q_3 = V_3 A_3 = (20)(0.2) = 4 \text{ ft}^3/\text{s}$

see part c on left side

Oil of specific gravity 0.83 flows in the pipe section shown. If viscous effects are assumed to be negligible, estimate the flow rate Q .



First note Pts 1 and 2 on the diagram and then write Bernoulli's eqn from ① → ②

$$\frac{P_1}{\gamma_{oil}} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma_{oil}} + \frac{V_2^2}{2g} + z_2 \quad \left\{ \begin{array}{l} z_1 = z_2 \\ V_1 = 0 \text{ stagnation point} \end{array} \right.$$

$$\therefore \frac{V_2^2}{2g} = \frac{P_1 - P_2}{0.83 \gamma_w}$$

$$V_2^2 = 2.410 g \frac{P_1 - P_2}{\gamma_w}$$

Now from the manometer eqn

$$P_1 - \gamma_{oil} h - \gamma_w \left(\frac{1}{3} \text{ ft}\right) + \gamma_{oil} \left(\frac{1}{3} \text{ ft}\right) + \gamma_{oil} h = P_2$$

$$P_1 - P_2 = \gamma_w \left(\frac{1}{3} \text{ ft}\right) (1 - 0.83)$$

$$\frac{P_1 - P_2}{\gamma_w} = \left(\frac{1}{3} \text{ ft}\right) (0.17) = 0.05667 \text{ ft}$$

$$\therefore V_2 = \left[2.410 \left(32.174 \frac{\text{ft}}{\text{s}^2}\right) (0.05667 \text{ ft}) \right]^{1/2}$$

$$V_2 = 2.096 \text{ ft/s}$$

and finally

$$Q = V_2 A_2 = \left(2.096 \frac{\text{ft}}{\text{s}}\right) \frac{\pi}{4} \left(\frac{1}{3} \text{ ft}\right)^2 = 0.183 \text{ ft}^3/\text{s}$$