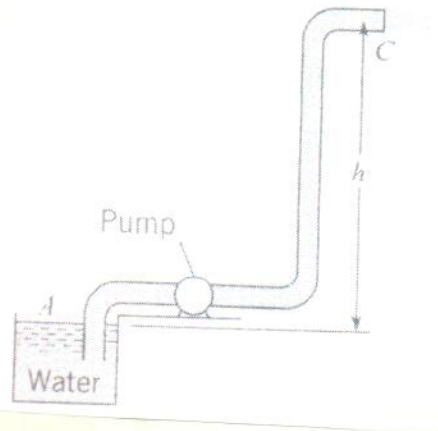


7.34 A pump draws water through a 20 cm suction pipe and discharges it through a 15 cm pipe which has a flow velocity of 5 m/s. To what height, h , above the water surface at pt. A can the water be raised if 35 kW of power is delivered to the pump?



Assume that the pump operates at 70% efficiency and that the head loss in the pipe between pts A and C is equal to $2V_c^2/2g$.

35 kW pump is used

reword slightly

The energy eqn between pts A and C is

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A + h_A - h_f - h_L = \frac{P_C}{\gamma} + \frac{V_C^2}{2g} + z_C$$

\leftarrow free surface \leftarrow free surface \leftarrow free jet

$$\therefore h = z_C - z_A = h_A - h_L - \frac{V_C^2}{2g} = h_A - \frac{3V_C^2}{2g}$$

but $h_L = \frac{2V_C^2}{2g}$

also

$$Q = A_C V_C = \frac{\pi}{4} (0.15 \text{ m})^2 \left(\frac{5 \text{ m}}{\text{s}} \right) = (0.01767 \text{ m}^2) \left(\frac{5 \text{ m}}{\text{s}} \right) = 0.08836 \text{ m}^3/\text{s}$$

$$P_A = \eta P_s = 0.70 (35 \text{ kW}) = 24.5 \text{ kW}$$

power added to fluid

$$h_A = \frac{P_A}{\gamma Q} = \frac{24.5 \text{ kW}}{(9.81 \frac{\text{kN}}{\text{m}^3}) (0.08836 \text{ m}^3/\text{s})} = 28.26 \text{ m}$$

units

$$\frac{\text{kW} \cdot \text{m}}{\frac{\text{kN}}{\text{m}^3} \cdot \frac{\text{m}^3}{\text{s}}} = \text{m}$$

$$\frac{V_C^2}{2g} = \frac{(5 \text{ m/s})^2}{2(9.8 \text{ m/s}^2)} = 1.276 \text{ m}$$

$$\therefore h = 28.26 \text{ m} - 3(1.276 \text{ m}) = 24.48 \text{ m} \Rightarrow 24.5 \text{ m}$$